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Flow banding in obsidian: A record of evolving textural heterogeneity during magma deformation

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Abstract

We perform a quantitative textural analysis of banding in obsidian from Big Glass Mountain (BGM), Medicine Lake Volcano, California and from Mayor Island (MI), New Zealand. The samples are compositionally homogeneous, with banding defined by variable microlite content (BGM) or vesicularity (MI). The spatial distribution of alternating light and dark bands has a $1/\text{wavenumber}$ power-spectral density, as well as multifractal characteristics. Through the use of simple mathematical models, we demonstrate that formation of the observed banding structure is consistent with a continuous deformational reworking of magma. Our results indicate that changes in crystallinity (vesicularity) were concurrent with magma deformation and are random multiples of the total amount of crystallinity (vesicularity) that was already present at any given time. Banded obsidian from BGM and MI can be found in close spatial proximity to brittle deformational textures. We therefore propose that a key element of banding formation in our samples may be magma brecciation or fragmentation. Fragmentation can result in variable rates of degassing of fragments, which in turn can lead to nonuniform crystal (vesicle) nucleation and growth rates. Repeated fragmentation, welding and subsequent viscous deformation can thus lead to banding formation.

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1. Introduction

Banding in obsidian samples from Big Glass Mountain (BGM), Medicine Lake Volcano, California and from Mayor Island (MI), New Zealand preserves a record of deformation associated with magma ascent, eruption, and emplacement. Alternating light and dark bands ranging in width from tens of microns to

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decimeters are defined by differences in crystallinity (BGM) or vesicularity (MI). Proposed processes for banding formation include viscous magma mixing (e.g., [1–4]), repeated autobrecciation and welding of fragments during flow at the surface (e.g., [5,6]), welding and rheomorphism of pyroclastic fragments (e.g., [7–11]), vapor-precipitated crystallization in stretched vesicles [12], or brittle deformation and welding of fragments during magma ascent in the volcanic conduit [13–16].

Although textural heterogeneity caused by mixing of preexisting parent magmas has received considerable attention, the origin of compositionally homogeneous banded lavas, such as BGM or MI samples, remains relatively unexplored. This is an important area of study because crystal or bubble nucleation and growth are intimately linked to magma degassing [17–19], which in turn is responsible for the buildup of overpressure required for the transition from effusive to explosive eruptive behavior [20–25]. One important unanswered question is whether the deformational process that results in banding is separate from (i.e., subsequent to) the actual development of textural heterogeneity or if both processes are related in some manner.

2. Approach

The main goal of our analysis is to assess whether banding in the BGM and MI obsidian samples preserves a record from which we can gain insight into the general nature of the underlying formational process, and hence about magma ascent and emplacement processes inaccessible to direct observation. We use spectral and multifractal analyses of banding to test if the formation of textural heterogeneity occurred prior to deformation, or if both processes are concurrent. We focus on obsidian because the optical transparency allows measurements of structures to be made over a broad range of scales. Moreover, the obsidian samples under consideration bear evidence of a genetic relation between brittle magma deformation and banding formation. A petrographic description of both samples is provided in Section 3.

In Section 4 we describe the results from power-spectral and multifractal analyses of each sample. Powerspectral analysis permits the identification of a

scale-invariant record, whereas multifractal analysis allows the identification of a multiplicative formational process. In the context of the two samples analyzed here, this corresponds to a repeated (continuous) change in crystallinity (BGM) or vesicularity (MI) that is a small random multiple of the total amount already present. Such a process is called multiplicative and, in contrast to cumulative processes, results in binomial frequency distribution of the given attribute. Using a series of hypothesis tests (Section 5), we provide constraints on the required dynamics of such a process. Finally, in Section 6 we discuss brittle deformation of magma as a possible physical mechanism for the formation of banding in BGM and MI obsidian samples.

3. Samples

Banding in BGM and MI obsidian is defined by alternating planar layers of varying color as a consequence of varying microrystallinity (BGM) or microvesicularity (MI). In cross-section this layering ranges in thickness from microns to decimeters and may attain lengths of up to several meters. Often, the layering can be distorted or folded [26].

3.1. BGM obsidian

BGM is a 900-year-old rhyolite-to-dacite obsidian flow [27–30]. It is the youngest part of the Medicine

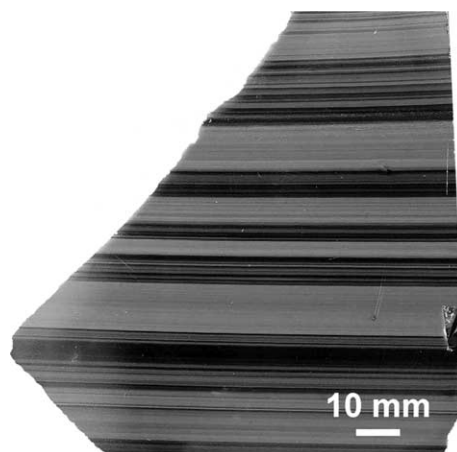


Fig. 1. Photograph of banded obsidian sample from Big Glass Mountain, Medicine Lake Volcano, California.

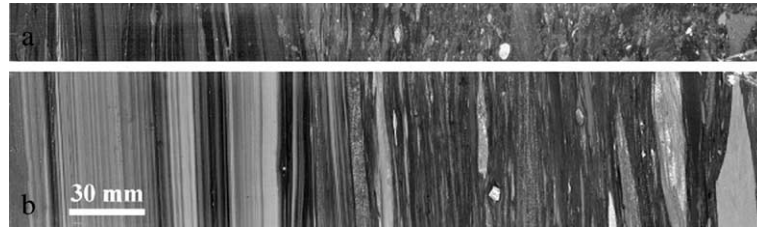


Fig. 2. Two different views of the same sample of obsidian from Big Glass Mountain. The sample is a rectangular slab and (a) is the side view perpendicular to (b). The sample shows a continuous gradation from angular, fused fragments (right third), to deformed fragments (middle), to well-developed banding (left third), consistent with brittle deformation, welding of fragments and subsequent viscous deformation.

Lake composite shield volcano [27] and provides an example of the effusive emplacement of a cubic kilometer-sized volume of silicic melt. Effusion was preceded by an explosive phase that resulted in the deposition of tephra over an area of approximately 320 km² [31]. BGM therefore provides an excellent example of a sizable silicic eruption with a transition from explosive to effusive behavior. The youngest eruptive sequence includes obsidian that is ubiquitously banded (Fig. 1), with some samples bearing evidence for a genetic relation between fragmentation and banding (Fig. 2).

Banding is predominantly defined by varying concentrations of pyroxene microlites (Fig. 3), with a higher microlite content resulting in a darker color. At times, dark bands also contain increased concentrations of oxides (e.g., the darkest band in Fig. 3). However, overall there appears to be no compositional difference or difference in water content (J. Castro, personal communication) between individual bands of BGM obsidian. Some samples show a continuous gradation from angular, fused fragments (right third of Fig. 2), to deformed fragments (middle of Fig. 2), to well-developed banding (left third of Fig. 2), indi-

cating that brittle deformation, welding of fragments and subsequent deformation may have resulted in at least some of the observed banding.

3.2. MI obsidian

MI is the visible portion of a 700-m-high and 15-km-wide Quaternary shield volcano [32]. Despite its uniform peralkaline magma composition, MI's history includes virtually the full range of known eruption styles over a wide range of eruption sizes [33,34], including fire-fountaining and spatter-fed lava flows, such as the 8-ka obsidian flow from which our sample was collected [7,10,34]. Banding in the MI obsidian sample under consideration is predominantly defined

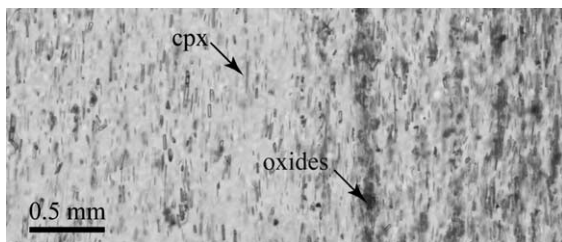


Fig. 3. Photomicrograph of obsidian from Big Glass Mountain. Banding is generally defined by varying microlite content in a glassy matrix. Some dark bands also contain oxides.

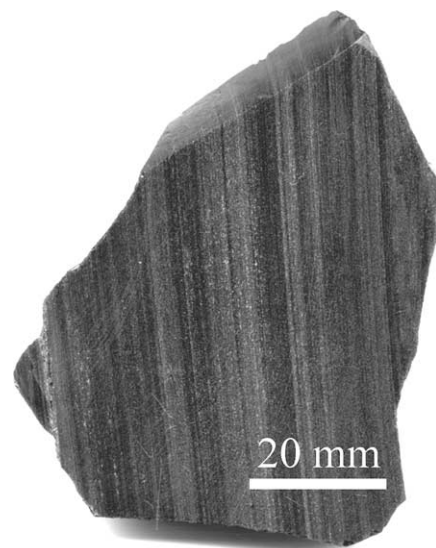


Fig. 4. Polished sample of Mayor Island banded obsidian (provided by K. V. Cashman, University of Oregon).

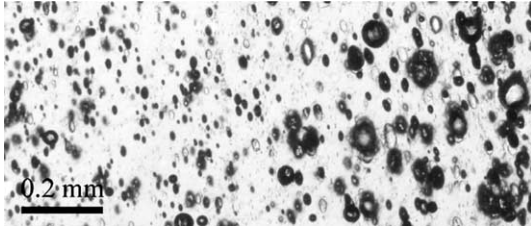


Fig. 5. Photomicrograph of obsidian from Mayor Island. Banding is defined by varying vesicularity.

by varying bubble content (Figs. 4 and 5), with higher vesicularity corresponding to lighter bands. The MI sample provides a sample of banded obsidian with evidence of a clastogenic origin and close spatial association with magma brecciation [7].

3.3. Digitized banding

Our subsequent analysis is based on photomicrographs of polished obsidian samples. Because of the degree of magnification, each analyzed sample image actually represents a composite of a number of high-resolution digital photographs. The digitized sample from BGM has a length of 200 mm and a resolution of 2 $\mu\text{m}/\text{pixel}$ (Fig. 6a). Equivalently, we obtain a digital record with 5 $\mu\text{m}/\text{pixel}$ resolution from a 55-mm-long sample of MI obsidian, provided by K. V. Cashman, University of Oregon (Fig. 6b). The cumulative frequency distribution of resultant gray-scale color index values, $0 \leq C_i \leq 1$, from each sample is shown in Fig. 7. Consistent with the terminology used in multifractal analysis, each digitized sample will hereafter be referred to as the “record.”

We normalize gray-scale color index, C_i , for each pixel, i , as

$$\phi_i = [C_i - \min(C)] \left[\sum_{i=1}^N C_i - N\min(C) \right]^{-1}$$

where $\sum_{i=1}^N \phi_i = 1$. (1)

Here ϕ_i is the normalized gray-scale color index, hereafter also referred to as the “measure.” It is not our goal to draw detailed quantitative estimates of process parameters from our analysis. Instead we only seek to establish if BGM and MI samples are

multifractal or not. Unlike for example Perugini et al. [4], where bands are defined by compositional variations, we do not obtain a precise calibration of color index to microcrystallinity or microvesicularity of our samples. It should be noted that, our transformation from natural samples to measures does not bias the outcome of our analysis, as will be shown in Section 5.

4. Analysis of banding

4.1. Power spectrum

The wavenumber power spectrum, $S(k)$, is one of the most often used tools for studying complex spatial patterns, because of its compact quantitative description of the presence of many spatial scales [35]. We use the multitaper method (e.g., [36] and references therein) as a spectral estimator, where data windows are given by discrete prolate spheroidal sequences [37] that effectively minimize spectral leakage. This technique is well suited for detailed spectra with a large dynamic range. We tested different taper sequences to minimize leakage effects or other artifacts and find that an estimator with $NW=4$ (time bandwidth for the Slepian sequences) is well suited for our analysis. Both BGM and MI spectra (Fig. 8) are characterized by a $1/\text{wavenumber}$ scaling of spectral power, $S(k) \sim k^{-1}$, indicating scale invariance.

4.2. Multifractal analysis

Monofractal records are often characterized by k^{-1} power spectra. They have the same scaling properties throughout the entire signal and can be characterized by a single fractal dimension. Records produced by multiplicative processes, in contrast, are usually found to be multifractal [38,39]. Instead of being characterized by a single fractal dimension, they have locally varying scaling properties that contain valuable information regarding the formational process (e.g., [39]). For example, the energy-cascading process embodied by fluid turbulence generates a multifractal time series of velocity fluctuations that is mathematically well represented by a multiplicative model [39]. We therefore use a multi-

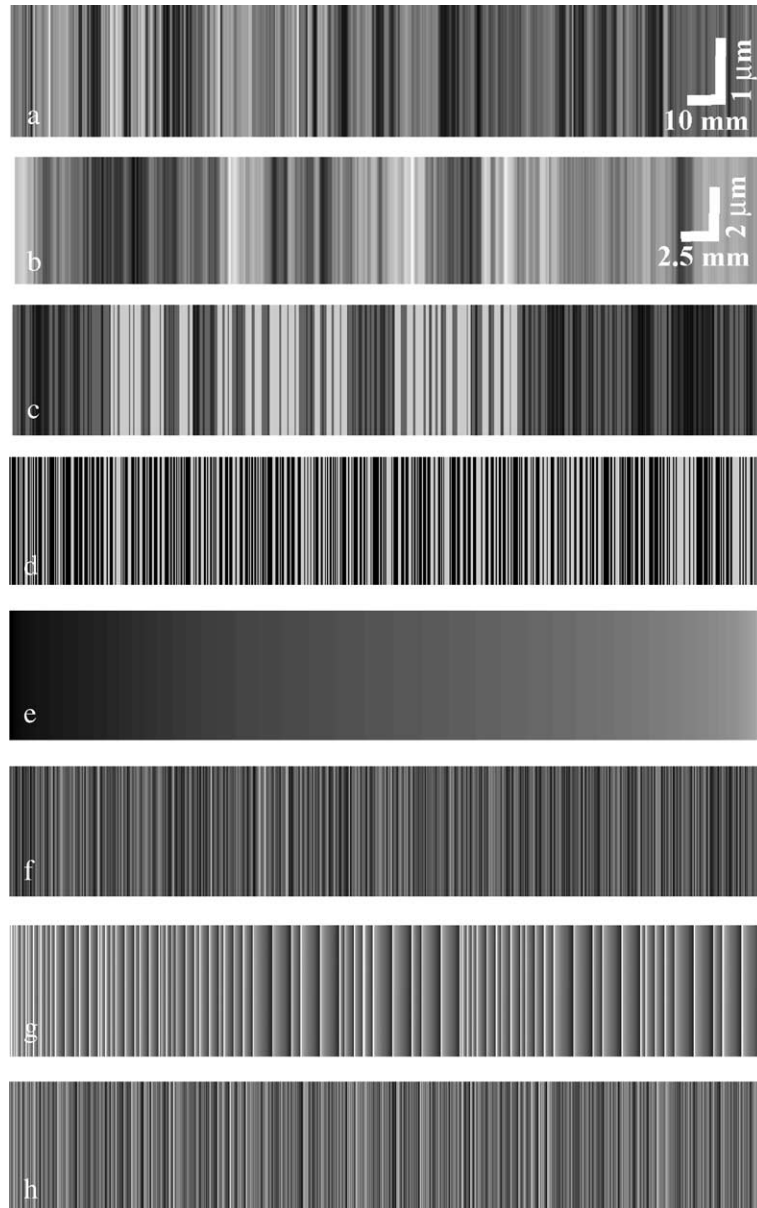


Fig. 6. Banding for (a) Big Glass Mountain (BGM) (200 mm length), (b) Mayor Island (55 mm length), (c) Multiplicative cascade (MC) based on the two-scale cantor set, (d) MC with alternating black and white bands only, (e) BGM pixels sorted by color index, (f) BGM with random redistribution of pixels, (g) Baker's map of the sorted BGM from panel (e) after four iterations, (h) Baker's map of sorted BGM from panel (e) after six iterations.

fractal analysis to test whether banding in BGM and MI obsidian is multifractal and, hence, possibly preserves a record of a multiplicative formational process.

4.2.1. Method

Multifractal records can be characterized by the singularity spectrum, $f(\alpha)$, of some measure, $\phi(x)$, which in our case represents the normalized color

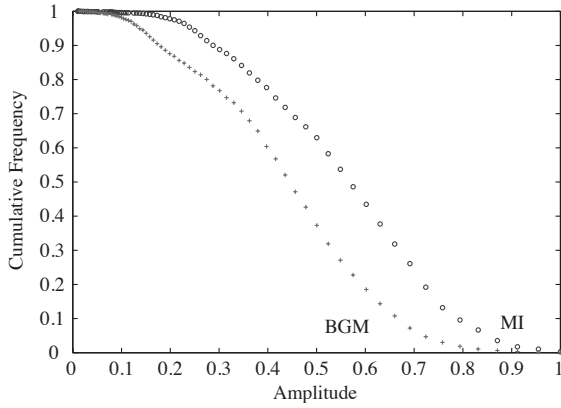


Fig. 7. Cumulative frequency distribution of the measure (normalized gray-scale color index) for Big Glass Mountain and Mayor Island obsidian samples.

index as a proxy for microcrystallinity (BGM) or vesicularity (MI). It is possible to evaluate the presence of different scaling laws throughout the record via the integrated measure

$$\mu_i = \int_{i-L/2}^{i+L/2} \phi dx, \text{ where } \sum_{i=1}^N \mu_i = 1. \quad (2)$$

Here L is the length of a record segment centered at position i , with the entire record of length X subdivided into $N=X/L$ segments. The $f(\alpha)$ singularity-spectrum provides a mathematical description of the spatial distribution of ϕ over the entire record, with the singularity strength, α , defined by

$$\mu_i(L) \sim L_i^\alpha. \quad (3)$$

Counting the number of segments, $N(\alpha)$, where $\mu_i(L)$ has a singularity strength, α , allows the loose definition of $f(\alpha)$ as the fractal (Hausdorff) dimension of the part of the record with singularity strength of α [38,40]

$$N(\alpha) \sim L^{-f(\alpha)}. \quad (4)$$

For a given segmentation length, or an equivalent box-counting dimension, L , the value of α will vary with position i . As a consequence, $f(\alpha)$ characterizes the spatial complexity of the actual record. If the record is uniformly fractal (monofractal) or not fractal at all, then there will be only one value of α , reducing $f(\alpha)$ to a single point. If the record is

complexly (though not randomly) structured so that its fractal dimension changes with position, then there exists a range of α with different Hausdorff dimensions, $f(\alpha)$. The more complexly structured the record is, the broader the spectrum will be.

The spectrum $f(\alpha)$ can be obtained by considering different moments, μ_i^q , of the integrated measure. Here the parameter ϕ provides a “microscope” for exploring different regions of the banding structure. As ϕ is varied, different subsets of the record, which are associated with different scaling exponents, α , become dominant. The singularity spectrum can then be obtained from [40]

$$f(q) = \lim_{L \rightarrow 0} \frac{\sum_i \mu_i^q(L) \log[\mu_i^q(q, L)]}{\log L} \quad (5)$$

and

$$\alpha(q) = \lim_{L \rightarrow 0} \frac{\sum_i \mu_i^q(L) \log[\mu_i(L)]}{\log L}. \quad (6)$$

In practice, the slopes of $\sum_i \mu_i^q(L) \log[\mu_i^q(q, L)]$ and $\sum_i \mu_i^q(L) \log[\mu_i(L)]$ versus $\log L$ are estimated to obtain $f(\alpha)$ and α , respectively. In multifractal analysis there are a number of potential problems that must be avoided ([41] and references therein). Most importantly, care must be taken to only consider the range of $\log L$ over which these graphs do actually represent

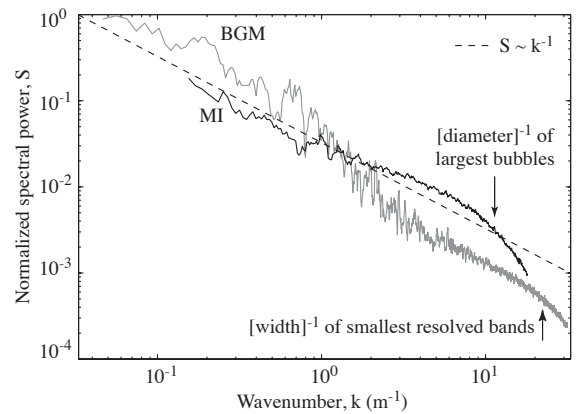


Fig. 8. Power spectra for Big Glass Mountain and Mayor Island obtained from averaging the spectra from 200 rasters of the digital photomicrograph of each obsidian sample. Both spectra are characterized by a $1/\text{wavenumber}$ scaling of spectral power ($S(k) \sim k^{-1}$) indicating scale invariance.

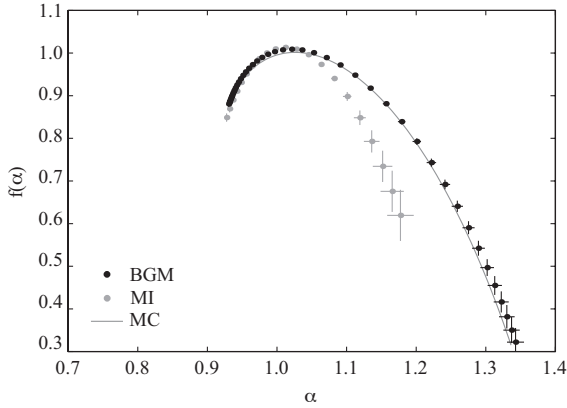


Fig. 9. Singularity spectra obtain by the Chhabra–Jensen method [40]. $f(\alpha)$ for Big Glass Mountain (BGM) and Mayor Island (MI) are broad, indicating a multifractal record. The error of estimation is evaluated from the variance in the estimation of the slope (Section 4.2.1). Also shown is the multifractal singularity spectrum for the multiplicative cascade generated via the two-scale Cantor set [38]. Both BGM and MI singularity spectra are consistent with a multiplicative process.

linear trends. If they do not represent linear trends, then the record is not truly multifractal, but could still result in a singularity spectrum with multifractal char-

acter. Therefore, $f(q)$ and $\alpha(q)$ were estimated for $\max(\delta_{\text{BGM}}, \delta_{\text{MI}}) \leq L \leq \min(X_{\text{BGM}}, X_{\text{MI}})/10$. Here δ_{BGM} represents the width of the smallest resolved band of the BGM sample, δ_{MI} is the average diameter of the largest bubbles of the MI sample, X_{BGM} is the length of the BGM sample, and X_{MI} is the length of the MI sample. These ranges correspond to linear segments of the aforementioned graphs and are identical for both samples, so that there is no bias in the analysis. Furthermore, it should be noted that we compared our results for the entire BGM sample (200 mm in length) with analyses of segments of the BGM sample with lengths identical to that of the MI sample (55 mm). In all cases, the BGM singularity spectrum essentially has the multifractal characteristics shown in Fig. 9. Finally, we compared results from the Chhabra–Jensen method with the Legendre-transform method [38] and found the results shown here to be robust.

4.2.2. Results

The singularity spectrum (Fig. 9) indicates that banding structure of BGM and MI obsidian are multifractal, implying that banding may have formed

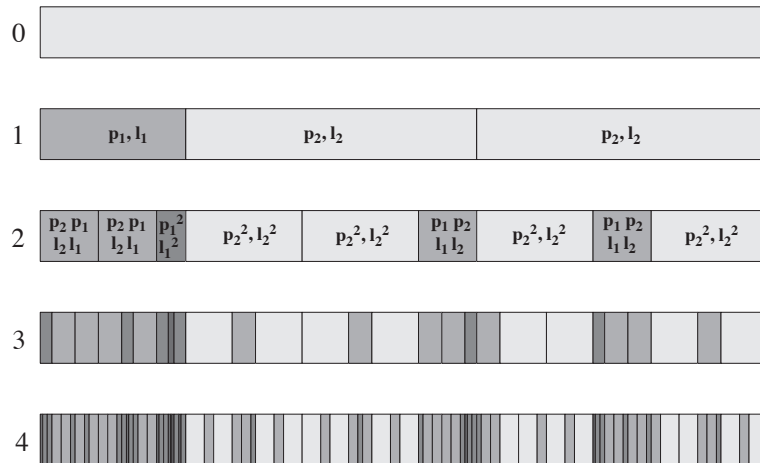


Fig. 10. Multifractal record generated by a multiplicative cascade (after four iterations) based on the two-scale Cantor set [38]. The segment of unit length and uniform measure (denoted by gray-scale color) shown at step 0 is cut into three segments, one of length l_1 and two of length l_2 . The measure of the first segment is multiplied by a factor of p_1 , and that of the two other segments is multiplied by a factor of p_2 , where $p_1 > p_2$. Each of the resulting three segments shown at step 1 are, in turn, cut into three segments, one of length $l_1 l_{\text{seg}}$ and two of length $l_2 l_{\text{seg}}$. Here l_{seg} denotes the length of the given segment shown at step 1. The resultant segment lengths are either $l_1 l_2, l_1^2$, or l_2^2 . Concurrently, the measure of each segment from step 1 is again multiplied by either p_1 if its length is $l_1 l_{\text{seg}}$, or by p_2 otherwise. The resultant segments and measures, denoted by different shades of gray ($p_1 p_2, p_1^2$, or p_2^2), are shown at step 2. The process is then repeated for steps 3 and 4. It should be noted that the spatial sequence into which each segment is subdivided is chosen randomly at any given step.

Table 1
Comparison of obsidian samples

Record	MF ^a	($S \sim k^{-1}$) ^b	MP ^c	Implications
Big Glass Mountain (BGM)	Y	Y	Y	Concurrent microlite growth and deformation into bands
Mayor Island (MI)	Y	Y	Y	Concurrent formation of variable vesicularity and deformation
Cantor (MC)	Y	Y	Y	Concurrent development of heterogeneity and deformation
Cantor binary	N	N	N	No binomial measure
BGM randomized	N	N	N	Decoupled microlite growth and deformation into bands
Baker's map	Y	N	N	Decoupled microlite growth and deformation into bands

Cantor map with hypothesis tests.

^a Multifractal.

^b S is spectral power and k is wavenumber.

^c Multiplicative process.

through a multiplicative processes. To illustrate that this is feasible, we show $f(\alpha)$ for a multifractal record produced by a simple mathematical model representative of a multiplicative processes (Fig. 9). It is based on the two-scale Cantor set (MC) [38], where a unit interval is randomly subdivided into three segments: two of given length l_2 , and one of length l_1 (Fig. 10). The two former intervals each receive a proportion, p_2 , of the total measure, and the latter interval receives a proportion given by p_1 , as indicated by the different color shading. This process is recursively repeated for each segment from the previous iteration (Fig. 10). In an idealized sense this could, for example, be equivalent to a fragmentation process with a given scaling for fragment sizes (l_1 and l_2) and an embedded enrichment or depletion (p_1 and p_2) of some measure (e.g., volatile content, crystal or vesicle content, chemical or isotopic component). This idealized multiplicative process with $l_1 = p_1 = 1/5$ and $l_1 + 2l_2 = p_1 + 2p_2 = 1$ results in the banding shown in Fig. 6c and provides an excellent match to the BGM singularity spectrum (Fig. 9). It is important to note, that this implies that microcrystallinity (vesicularity) evolved concurrently to and integral with magma deformation in BGM (MI) obsidian.

5. Alternative hypotheses

To assess the limitations of our results, we test several alternative hypotheses, summarized in Table 1.

5.1. Black and white banding

Fig. 6d shows the banding structure generated by the same multiplicative process as shown in Fig. 10, but with banding defined by only two alternating values of the measure ϕ (black or white). In contrast to the BGM and MI samples, as well as the MC model, this binary banding is not multifractal, and its singularity spectrum consists of a single point, shown in Fig. 11. As already discussed by Turcotte [42], this demonstrates the importance of a binomial measure produced through a multiplicative enrichment or fractionation process in the generation of a multifractal record (e.g., [43–45]).

5.2. Randomized BGM

Fig. 6e shows the banding of the BGM sample (Fig. 6a), but sorted from darkest to lightest normalized color index, ϕ . For our second test, we randomly redistributed this measure. This hypothesis is motivated by the possibility that microlite content or

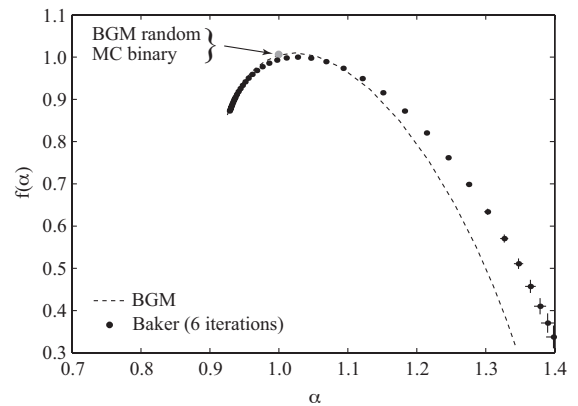


Fig. 11. Singularity spectra for the different hypothesis tests. Big Glass Mountain with randomized pixels (Fig. 6f) and the multiplicative cascade with only black-and-white bands (Fig. 6d) are monofractal and plot as single points. The spectrum for the generalized Baker's map after six iterations (Fig. 6g) is multifractal and similar to that of the Big Glass Mountain sample (Fig. 6a), shown as the dashed line.

vesicularity may vary, for example, radially or vertically before the actual mixing process, as suggested by Castro and Mercer [46]. In this case the “mixing” process is of a purely random nature (as opposed to chaotic or otherwise). The resultant record (Fig. 6f) is not multifractal (Fig. 11). We can conclude that a binomial measure alone does not suffice for a multifractal record, implying that a random formational process, or random “mixing” of a preexisting measure, is not sufficient for the formation of multifractal banding.

5.3. Chaotic mixing via Baker’s map

In our third test, we examine the possibility that a preexisting measure (e.g., microlite content) of identical probability distribution as the BGM sample (Fig. 6e) could be redistributed through a chaotic mixing process to result in banding with similar characteristics as the BGM sample. Similar to Section 5.2, this hypothesis is motivated by the possibility of a preexisting gradation in microlite content or vesicularity prior the actual mixing process [46].

A simple mathematical model that has been used to represent the characteristics of chaotic mixing is the generalized Baker’s map (e.g., [35,47,48]). We performed calculations using several different parameterizations of the generalized Baker’s map. Although details varied between different versions, the overall results were the same. We therefore only show results for one version of this map. This version has a ratio of segmentation lengths identical to that of the multiplicative Cantor process (Fig. 10). The Baker’s map spatially redistributes a given measure on a unit square and is mathematically equivalent to the process of stretching and folding in chaotic fluid mixing,

illustrated in Fig. 12. Mathematically, the process is given by the mapping

$$\begin{aligned} x_{n+1} &= \begin{cases} l_2^* x_n, y_n / l_2^* & \text{if } y_n < l_2^* \\ l_2^* + l_1^* x_n, (y_n - l_2^*) / l_1^* & \text{if } l_2^* < y_n \leq l_2^* + l_1^* \\ l_2^* + l_1^* + l_1^* x_n, (y_n - l_2^* - l_1^*) / l_1^* & \text{if } l_2^* + l_1^* < y_n. \end{cases} \end{aligned} \tag{7}$$

Here $l_1^* = l_1 + \theta$, $l_2^* = (1 - l_1^*) / 2$, and θ is a number chosen randomly at each iteration, with $\theta \leq l_1 / 2 \leq \theta$. The Baker’s map is analogous to closed-system chaotic mixing, in which the original measure is conserved throughout (i.e., for all iterations $\sum_{i=1}^N \phi_i = 1$). With respect to BGM (MI), the Baker’s map implies that microlite (vesicle) growth and banding formation are decoupled. The singularity spectrum (Fig. 9) obtained from this map is multifractal and is very similar to the BGM sample (Fig. 11). However, the power spectrum allows a clear distinction. Whereas power spectra of BGM, MI (Fig. 8), and the MC model are characterized by $S \sim k^{-1}$, the power spectrum for the Baker’s map with initial measure derived from the BGM sample has $S \sim k^{-\beta}$, with $\beta \approx 1.5 - 2$. This result indicates, consistent with results from mixing studies (e.g., [4,47,48]), that a magma with preexisting nonuniform microlite content, or vesicularity, can be mixed, resulting in banding with multifractal properties. However, the power spectrum is not likely to have the $S \sim k^{-1}$ scaling observed in BGM and MI samples.

5.4. Summary

The results of the hypothesis tests, summarized in Table 1, demonstrate (1) that banding has to be defined by binomial frequency distribution of textural heterogeneity (Section 5.1); and (2) that spatial redis-

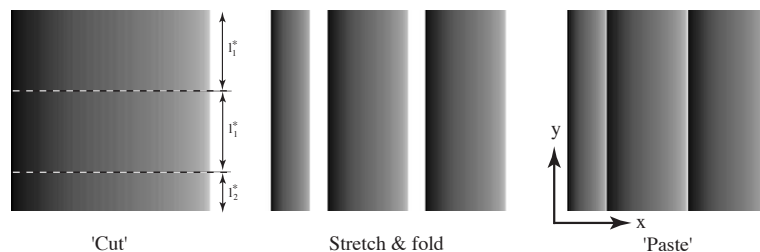


Fig. 12. Schematic representation of the modified Baker’s map (e.g., [47,48]), where the initial measure is based on the sorted Big Glass Mountain of Fig. 6e. This map represents a chaotic redistribution of a preexisting measure.

tribution of preexisting heterogeneity is insufficient to reproduce banding characteristics of BGM and MI samples (Sections 5.2 and 5.3). The latter also shows that using normalized gray-scale color index will not bias our results in terms of the multifractal vs. monofractal character of banding.

6. Application

We have shown that a multiplicative process, whereby the development of textural heterogeneity and the spatial redistribution thereof are concurrent and interrelated, is consistent with banding of obsidian samples from BGM and MI. The multiplicative cascade represented by the two-scale Cantor set (Fig. 10) embodies the multiplicative nature of an idealized physical process, but is not indicative of the mechanics of such a process. In this section we propose a hypothetical physical process that is multiplicative and consistent with the formation of banded obsidian. It consists of repeated cycles of brittle magma deformation followed by welding of fragments and subsequent viscous deformation into bands. A schematic illustration of this process is shown in Fig. 13.

6.1. Brittle deformation

Brittle deformation of magma occurs when strain rates locally exceed the ability of the melt to deform viscously [49–51], causing it to break into fragments like a brittle solid. This transition is referred to as the glass transition (e.g., [49–52]). Variable degassing of magma fragments may result in variable crystallization (vesiculation) kinetics [17–19,53] over relatively short distances. For example, microlite content, which defines banding in BGM obsidian samples, varies by less than a few volume percent [54], suggesting that realistic conditions (i.e., length and time scales) for the development of observable textural heterogeneity are not difficult to achieve.

Because of the displacement and rotational component associated with simple shear deformation, fragments from different spatial locations could easily become juxtaposed. Once strain rates have relaxed magma fragments can become welded and deformed viscously. Viscous deformation of texturally heterogeneous, welded fragments will then result in band-

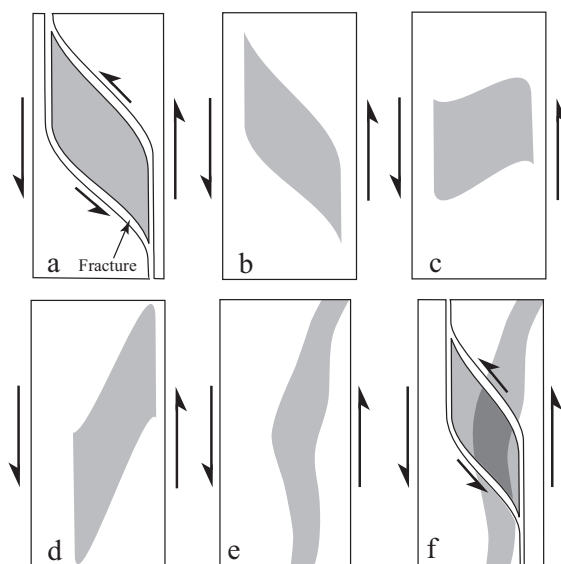


Fig. 13. Idealized schematic illustration of our conceptual model for banding formation via brittle deformation of magma. (a) Brittle deformation during simple shear. The single fragment shown here undergoes a change in texture (e.g., microlite content or vesicularity), indicated by the darker color. Note the presence of fractures and the sigmoidal geometry, which is similar to tension gashes. Tension gashes often form in en echelon arrays. They may be precursors to shear localization (e.g., [61] and references therein) and can be rotated by deformation either during or after formation. (b) The fragments have welded into one coherent piece. (c–e) Viscous deformation under simple shear into a band. (f) A second episode of fragmentation and multiplicative change in texture indicated by the change in color. Note that the band which formed during the previous cycle is broken into several pieces and becomes “reworked”. Repetition of this process will result in a broad range of textural heterogeneity and in an increasingly finer banding structure. The two-scale Cantor’s map (Fig. 10) is a simple one-dimensional representation of this process.

ing. This process may occur repeatedly (continuously) during ascent or surface emplacement of magma. It is, except for welding of fragments and viscous deformation, essentially equivalent to the comminution of rocks in fault or shear zones, where banding may also be observed [55].

Banding has been observed in close association with brittle deformation in BGM samples (Fig. 2), as well as at Mayor Island [7,10] and elsewhere (e.g., [5,6]). In addition, banding has also been observed within dissected conduits [15,56], indicating that, at least in some cases, banding may form during magma ascent in the conduit. Recent work suggests that shear strain rates during the ascent of silicic

magmas can exceed the glass transition [14,15,57], even for effusive eruptions that produce lava flows and domes. We therefore surmise that banding formation may occur both during ascent of silicic magmas and during surface emplacement.

6.2. Viscous deformation

Castro and Mercer [46] find that differences in the degree of volatile loss can account for some variability in microlite content in obsidian. However, they ultimately conclude that varying microlite content is more likely to record different ascent rates and residence histories in the volcanic conduit, rather than variations in magma degassing. They suggest that slower magma ascent rates near the conduit walls permit the development of higher crystallinity compared to that of faster ascending magma further in from the conduit walls. Similarly, it has been suggested that varying vesicularity may be caused by variable ascent rates [58], or by a spatially variable temperature distribution [59].

Pervasive banding formation over the observed spatial scales requires repeated stretching and folding, in which nearby parcels of magma can diverge strongly from each other. Unlike brittle deformation, the required divergent stretching is not easily achieved in a highly viscous magma without considerable complexity of the flow geometry (e.g., [60] and references therein). However, complexity of the flow during surface emplacement or in the upper parts of conduits may be more easily achieved than during ascent at depth within the volcanic conduit.

7. Conclusion

We conclude that the observed banding structure in BGM and MI obsidian is consistent with a repeated (or continuous) change in crystallinity or vesicularity that is a small random multiple of the amount already present. Moreover, this textural evolution was concurrent with, or integral to, the mechanical deformation of magma. Such a process creates increasingly finer scales of banding through a cascade to shorter and shorter wavelengths until some cutoff value, given by vesicle or crystal size, is reached [35]. We propose repeated cycles of magma brecciation, welding and

subsequent viscous deformation as a feasible mechanism for banding formation. This conceptual model is consistent with the concurrent development of textural heterogeneity through variable crystallization (vesiculation) kinetics as a consequence of variable degassing rates of magma fragments.

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